For each of the problems, show all your work. If it is not obvious what you are doing, briefly explain what steps you are taking to arrive at the solution.

## Problem 1

A non-inverting amplifier is made with an op-amp that is powered with $\pm 15 \mathrm{~V}$. The op-amp can be considered ideal, so that the usual rules of the op-amp apply.

The input voltage is fixed to 5 V , thus at the output of the op-amp we will have $\left(1+\frac{R_{1}}{R_{2}}\right) 5 \mathrm{~V}$.

a) Briefly explain why the current does not split up at the node between $R_{1}$ and $R_{2}$, i.e. why the current $I$ through $R_{2}$ is the same as through $R_{1}$.
b) How does the current $I$ change if $R_{2}$ is doubled and $R_{1}$ remains unchanged?
c) How does the current $I$ change if $R_{1}$ is doubled and $R_{2}$ remains unchanged?

Problem 2 (A modified version of 6.11 \#3 p. 273, second edition only)
Consider the circuit shown which is built from four resistors and an op-amp.
a) What is the voltage at the non-inverting opamp input ( $V+$ )? Express your result in terms of In terms of $V_{\text {out, }} R_{1}$ and $R_{2}$.
b) What is the input current to the circuit (current $I_{2}$ in the diagram). Express your result in terms of $V_{\text {in }}, V_{o u t}, R_{1}$ and $R_{2}$.
c) What is the voltage at the inverting op-amp input ( $V-$ )? Express your result in terms of $V_{\text {in, }} V_{\text {out, }} R_{1}$ and $R_{2}$.

c) By demanding that $V+=V-$, show that the output voltage of the circuit is $V_{\text {out }}=\frac{2 R_{2}}{R_{2} \quad R_{1}} V_{\text {in }}$

## Problem 3

A load resistor $R_{L}$ is connected to a voltage divider made of two resistors R1 and R2 as shown.
a) Find an expression for the voltage drop across the load resistor.
b) Let $\mathrm{Vo}=10 \mathrm{~V}, \mathrm{R} 1=\mathrm{R} 2=10 \mathrm{k} \Omega$ and $\mathrm{R}_{\mathrm{L}}=5 \mathrm{k} \Omega$. What happens to the voltage drop across the $5-\mathrm{k} \Omega$ load resistor if its value suddenly decreases to $2 \mathrm{k} \Omega$ ? Justify you answer with a calculation.

c) Now you add a voltage follower between the load resistor and the voltage divider as shown. Determine the voltage across the $5-\mathrm{k} \Omega$ load resistor. What happens to the voltage across the $5-\mathrm{k} \Omega$ resistor if it suddenly decreases to $3 \mathrm{k} \Omega$ ? Explain why this is different than in part b).


## Problem 4

a) Derive an expression for $V_{\text {out }}$ as a function of $V_{\text {in }}$, $R$ and $C$. Follow the same steps that we have taken in class with the integrator circuit (i.e. the circuit that had the capacitor in the feedback branch).
b) Suppose the square wave signal shown below is connected to the input of the circuit. Carefully
 draw a graph of the output voltage as a function of time. Use the attached sheet to construct your drawing. Be as quantitative as possible, using $R=2 \mathrm{k} \Omega$ and $\mathrm{C}=50 \mu \mathrm{~F}$, and assume the op-amp is powered with $\pm 12 \mathrm{~V}$.


